

любое триг ур-ие можно свести к ур-ию высших степеней

$$\text{tg } x = y$$

$$\sin^2 x = \sin^2 x / (\sin^2 x + \cos^2 x) = \sin^2 x / \cos^2 x (\sin^2 x / \cos^2 x + 1) =$$

$$= \sin^2 x / \cos^2 x \quad / \quad \cos^2 x (\sin^2 x / \cos^2 x + 1) / \cos^2 x =$$

$$= \text{tg}^2 x / (\text{tg}^2 x + 1) = y^2 / (y^2 + 1)$$

$$\cos^2 x = \cos^2 x / (\sin^2 x + \cos^2 x) = \cos^2 x / \cos^2 x (\sin^2 x / \cos^2 x + 1) =$$

$$= 1 / (\sin^2 x / \cos^2 x + 1) = 1 / (\text{tg}^2 x + 1) = 1 / (y^2 + 1)$$

$$\sin 2x = \sin 2x / (\sin^2 x + \cos^2 x) = 2 \sin x \cos x / (\sin^2 x + \cos^2 x) =$$

$$= 2 \sin x \cos x / \cos^2 x (\sin^2 x / \cos^2 x + 1) = 2 \sin x / \cos x \quad / \quad (\sin^2 x / \cos^2 x + 1) =$$

$$= 2 \text{tg} x / (\text{tg}^2 x + 1) = 2y / (y^2 + 1)$$

$$\cos 2x = \cos 2x / (\sin^2 x + \cos^2 x) = (\cos^2 x - \sin^2 x) / (\sin^2 x + \cos^2 x) =$$

$$= \cos^2 x (1 - \sin^2 x / \cos^2 x) / \cos^2 x (\sin^2 x / \cos^2 x + 1) = (1 - \text{tg}^2 x) / (1 + \text{tg}^2 x) =$$

$$= (1 - y^2) / (y^2 + 1)$$

$$\text{tg} 2x = \sin 2x / \cos 2x = 2 \text{tg} x / (\text{tg}^2 x + 1) \quad / \quad (1 - \text{tg}^2 x) / (1 + \text{tg}^2 x) =$$

$$2 \text{tg} x / (1 - \text{tg}^2 x) = 2y / (1 - y^2)$$

$$\text{tg} 3x = \text{tg}(x + 2x) = (\text{tg} x + \text{tg} 2x) / (1 - \text{tg} x \text{tg} 2x) = (\text{tg} x + 2 \text{tg} x / (1 - \text{tg}^2 x)) /$$

$$(1 - \text{tg} x \cdot 2 \text{tg} x / (1 - \text{tg}^2 x)) = ([\text{tg} x (1 - \text{tg}^2 x) + 2 \text{tg} x] / (1 - \text{tg}^2 x)) / (1 - 2 \text{tg}^2 x / (1 - \text{tg}^2 x)) =$$

$$= ([3 \text{tg} x - \text{tg}^3 x] / (1 - \text{tg}^2 x)) / (1 - 2 \text{tg}^2 x / (1 - \text{tg}^2 x)) =$$

$$= (3 \text{tg} x - \text{tg}^3 x) / (1 - \text{tg}^2 x - 2 \text{tg}^2 x) = (3 \text{tg} x - \text{tg}^3 x) / (1 - 3 \text{tg}^2 x) = (3y - y^3) / (1 - 3y^2)$$

$$A/B \quad / \quad C/B \quad = \quad A/C$$

$$\text{tg}(a+b) = \sin(a+b) / \cos(a+b) = (\sin a \cos b + \sin b \cos a) / (\cos a \cos b - \sin a \sin b)$$

$$= \cos a \cos b (\sin a / \cos a + \sin b / \cos b) / \cos a \cos b (1 - \sin a \sin b / \cos a \cos b) =$$

$$= (\sin a / \cos a + \sin b / \cos b) / (1 - \sin a \sin b / \cos a \cos b) = (\text{tga} + \text{tgb}) / (1 - \text{tga} \text{tgb})$$

$$3 \text{tg} 3x - \text{ctg} 2x = 4 \text{tg} x$$

$$3(3y - y^3) / (1 - 3y^2) - 1/2y \quad / \quad (1 - y^2) = 4y$$

$$(9y - 3y^3) / (1 - 3y^2) - (1 - y^2) / 2y - 4y = 0$$

$$[2y(9y - 3y^3) - (1 - 3y^2)(1 - y^2) - 4y \cdot 2y(1 - 3y^2)] / 2y(1 - 3y^2) = 0$$

$$[18y^2 - 6y^4 - 1 + y^2 + 3y^2 - 3y^4 - 8y^2 + 24y^4] / 2y(1 - 3y^2) = 0$$

$$[14y^2 - 1 + 15y^4] / 2y(1 - 3y^2) = 0$$

$$14y^2 - 1 + 15y^4 = 0$$

$$a = y^2$$

$$15a^2 + 14a - 1 = 0$$

$$D/4 = 49 + 15 = 64$$

$$a_1 = (-7 + 8) / 15 = 1/15$$

$$a_2 = (-7 - 8) / 15 = -1$$

$$y^2 = 1/15$$

$$y = \pm 1/\sqrt{15}$$

$$\text{tg} x = \pm 1/\sqrt{15}$$

$$x = \pm \arctg(1/\sqrt{15}) + Pk$$

$$2y(1 - 3y^2) \neq 0$$

$$y \neq 0$$

$$1 - 3y^2 \neq 0$$

$$3y^2 \neq 1$$

$$y \neq \pm 1/\sqrt{3}$$

$$\text{Answer: } \pm \arctg(1/\sqrt{15}) + Pk$$

